

Micro-randomized Trials & Mobile Health

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The Methodology Center
advancing methods, improving health



mHealth



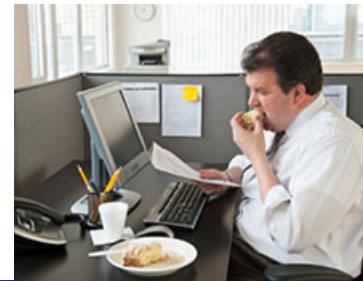
MD2K Smoking Cessation Coach

- Wearable bands measure activity, stress, cigarette smoking, sleep quality.....
- Smartphone provides four types of support 24/7
- Should wrist band provide supportive “cue” and smartphone activate to highlight associated support when stress reaches a criterion?

mHealth

HeartSteps Activity Coach

- Wearable bands measure activity, phone sensors measure busyness of calendar, location,.....
- Should smartphone ping and lockscreen deliver activity ideas when user is receptive and user's calendar is not too busy?



Data from wearable devices that sense and provide treatments

$$O_1, A_1, Y_2, \dots, O_j, A_j, Y_{j+1}, \dots$$

O_j : Observations at j^{th} decision time (high dimensional)

A_j : Action at j^{th} decision time (treatment)

Y_{j+1} : Proximal Response (aka, Reward, Cost, Utility)

Examples

- 1) Decision Times (Times at which a treatment can be provided.)
 - 1) Regular intervals in time (e.g. every 10 minutes)
 - 2) At user demand

HeartSteps includes two sets of decision times

- 1) Momentary: Approximately every 2-2.5 hours
- 2) Daily: Each evening at user specified time.

Examples

- 2) Observations S_j
 - 1) Passively collected (location, weather, busyness of calendar, social context, activity on device, physical activity)
 - 2) Actively collected (self-report)

HeartSteps includes activity recognition (walking, driving, standing/sitting), weather, location, calendar, adherence, step count, whether momentary intervention is on, self-report: usefulness, burden, self-efficacy, etc.

Examples

3) Actions A_j

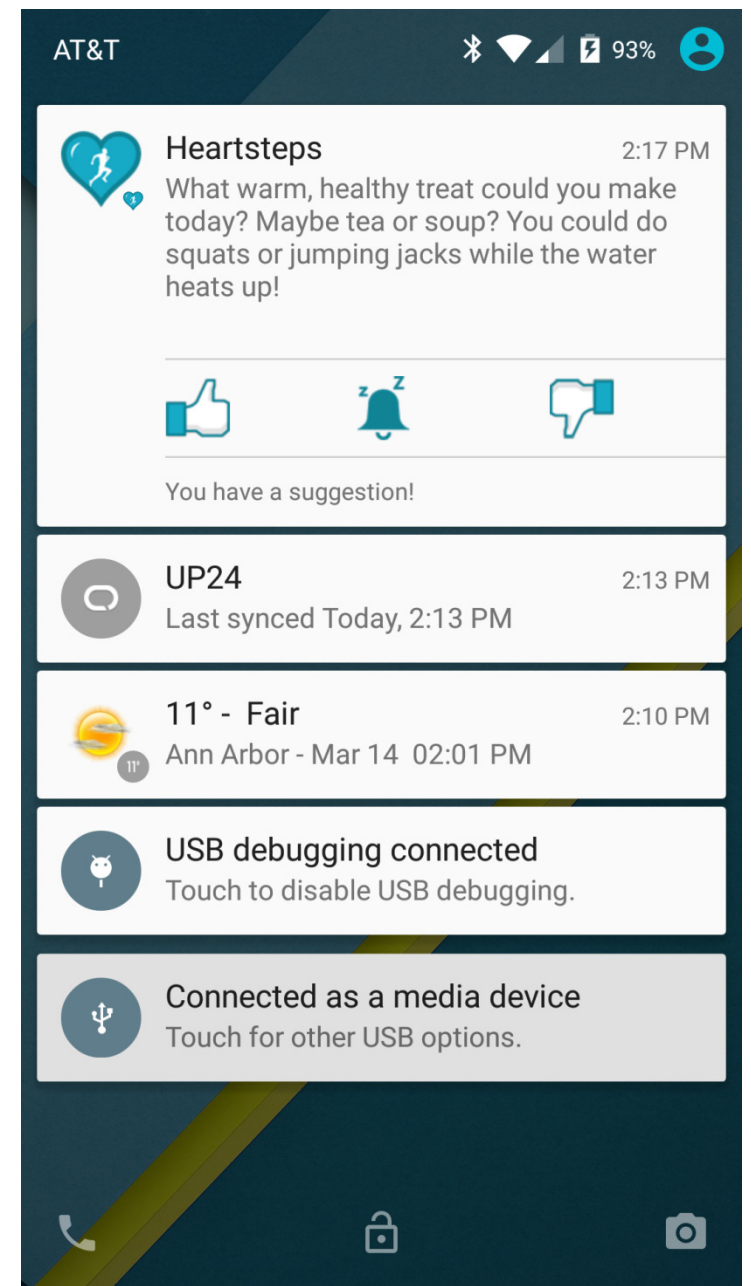
- 1) Treatments that can be provided at decision time
- 2) Whether to provide a treatment

HeartSteps includes two types of treatments

- 1) Momentary Lock Screen Recommendation
- 2) Daily Activity Planning

Momentary Lock Screen Recommendation

No Message or



Examples

4) Proximal Response Y_{j+1}

HeartSteps: Activity (step count) over next 60 minutes.

Smoking Cessation: Stress level over next x minutes.

Our Group's Scientific Goals

- 1) Develop trial designs/data analytics for assessing if there are proximal effects of the actions on the response.
- 2) Develop data analytics for assessing if there are delayed effects of the actions; assess if the effects vary by context, observations.
- 3) Develop data methods for constructing a treatment policy that inputs observations and delivers actions via phone.
- 4) Develop online training algorithms that will result in a Personalized Continually Learning mHealth Intervention

Proposed Experimental Design: Micro-Randomized Trial

Randomize between actions at decision times → Each person may be randomized 100's or 1000's of times.

These are sequential, “full factorial,” designs.

Why Micro-Randomization?

- Randomization (+ representative sample) is a gold standard in providing data to assess the causal effect of an intervention option.
- Sequential randomizations will enhance replicability and effectiveness of data-based decision rules.

Micro-Randomized Trial Elements

1. Record outcomes
 - Distal (scientific/clinical goal) & Proximal Response
2. Record context (sensor & self-report data)
3. Randomize among intervention options at decision points
4. Use resulting data to assess treatment effects, construct decision rules

Micro-Randomized Trial

- Focus on whether to provide a Momentary Lock Screen Recommendation, e.g.

$$A_j \in \{0, 1\}$$

- Randomization in HeartSteps

$$P[A_j = 1] = .4 \quad j = 1, \dots, J$$

Micro-Randomized Trial

First Question to Address: Do the intervention options have an effect on the proximal response?

--Test for proximal *main effects* of the intervention

Micro-Randomized Trial

Time varying potentially intensive intervention delivery → potential for accumulating habituation and burden



Allow proximal main effects of the intervention components to vary with time

Availability & The Main Effect

- Interventions can only be delivered at a decision time if an individual is *available*.
- The proximal main effect of treatment at a decision time is the difference in proximal response between *available* individuals assigned a lock-screen message and *available* individuals who are not assigned a lock-screen message.

Availability

- A_j is only delivered if the intervention is on at decision time j .
- Set $I_j = 1$ if the intervention is on at decision time j , otherwise $I_j = 0$

Potential Outcomes

- Define

$$\bar{A}_j = \{A_1, A_2, \dots, A_j\}, \bar{a}_j = \{a_1, a_2, \dots, a_j\}$$

- Define $Y_{j+1}(\bar{a}_j)$ to be the observed response, Y_{j+1} if $\bar{A}_j = \bar{a}_j$, e.g., $Y_{j+1} = Y_{j+1}(\bar{A}_j)$

- Define $I_j(\bar{a}_{j-1})$ to be the observed “intervention on” indicator if $\bar{A}_{j-1} = \bar{a}_{j-1}$

Proximal Main Effect

- The randomization implies that

$$E[Y_{j+1}(\bar{A}_{j-1}, 1) - Y_{j+1}(\bar{A}_{j-1}, 0) | I_j(\bar{A}_{j-1}) = 1] = \\ E[Y_{j+1} | I_j = 1, A_j = 1] - E[Y_{j+1} | I_j = 1, A_j = 0]$$

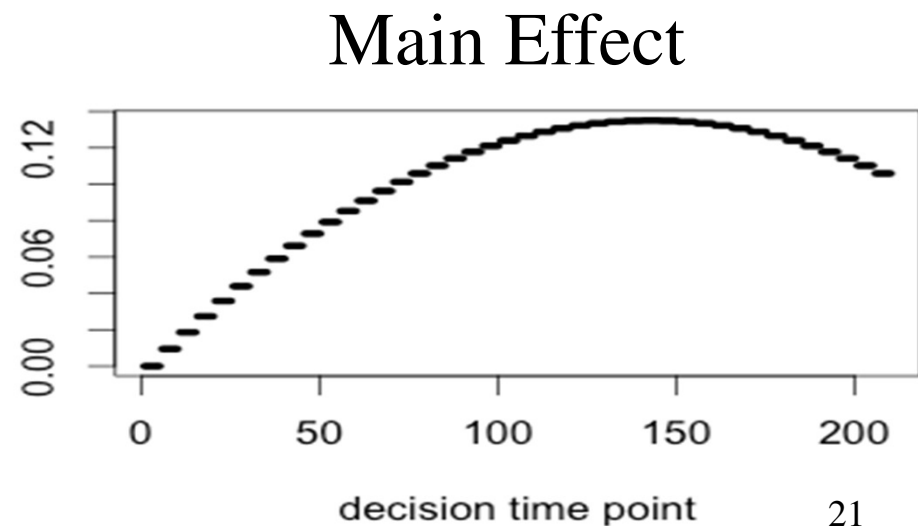
Proximal Main Effect

- The Proximal Main Effect at time j is

$$\beta(j) = E[Y_{j+1} | I_j = 1, A_j = 1] - E[Y_{j+1} | I_j = 1, A_j = 0]$$

- What does this estimand mean?

$\beta(j)$



Proposal

Design and size micro-randomized trial to detect proximal main effect of treatment

The proximal main effect is a time-varying main effect $\beta(j)$, $j=1, \dots, J$

The proximal main effect is a causal effect.

Sample Size Calculation

- We calculate a sample size to test:

$$H_0 : \beta(j) = 0, j = 1, 2, \dots, 210$$

- Size to detect a low dimensional alternative. E.g. $H_1: \beta(j)$ quadratic with intercept, β_0 , linear term, β_1 , and quadratic term β_2

$$\text{and test } \beta_0 = \beta_1 = \beta_2 = 0$$

Sample Size Calculation

Because the alternative hypothesis is low dimensional, assessment of the effect of the lock-screen message uses not only contrasts of *between person responses* but also contrasts of *within person responses*.

--The required sample size (number of subjects) will be small.

HeartSteps Sample Sizes

Power=.8, α =.05

**Standardized Average
Proximal Effect over
42 Days**

**Sample Size
For
70% availability or
50% availability**

0.06

81 or 112

0.08

48 or 65

0.10

33 or 43

Experimental Design Challenges

These are a new type of Factorial Design

- Time varying factors → time varying main effects, time-varying two-way interactions, different delayed effects
- Better Designs?
- Design Studies to Detect Interactions Between Factors.

Steps Toward Long-Term Goal

- 1) Develop methods/trial designs for assessing if there are proximal effects of the actions on the response.
- 2) Develop data analytics for assessing if there are delayed effects of the actions; assess if the effects vary by context/ observations.
- 3) Develop data methods, to use with batch data, for constructing a treatment policy that inputs observations and delivers actions via mobile device
- 4) Develop online training algorithms that will result in a “Continually Updating” Treatment Policy

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Current State

- Clinical scientists formulate mobile health intervention (e.g. treatment policy) using ideas from the literature, behavioral theory, clinical experience, observational data analyses.
- Develop analysis methods for use with data in constructing “evidence-based” treatment policies.
 - treatment policy should be interpretable.

Stochastic Treatment Policy

We aim to construct a parameterized policy, $\pi_{\theta}(a|s)$ that is bounded away from 0 and 1.

- Variation in actions can help retard habituation and maintain engagement.
- $\pi_{\theta}(a|s)$ that are continuous in θ are easier to estimate/compute.

Background

1) On each of n individuals data set contains:

$$S_1, A_1, Y_2, \dots, S_T, A_T, Y_{T+1}$$

-- S_t is a summary of $O_1, A_1, Y_2, \dots, Y_t, O_t$ that permits the Markovian property; a modeling assumption.

$$-- P[A_t = a | S_t = s] = \mu(a|s)$$

2) Optimality Criterion: Average Reward for Markov Decision Process

Markov Decision Process (MDP)

Markovian Assumptions

$$P[S_{j+1} = s' | S_1, A_1, \dots, S_j, A_j] =$$

$$P[S_{j+1} = s' | S_j, A_j]$$

and

$$P[Y_{j+1} = r | S_1, A_1, \dots, S_j, A_j] =$$

$$P[Y_{j+1} = r | S_j, A_j]$$

Stationarity Assumptions

$$P[S_{j+1} = s' | S_j = s, A_j = a] = p(s' | s, a)$$

and

$$E[Y_{j+1} | S_j = s, A_j = a] = r(s, a)$$

Optimality Criterion

Average Reward, η_θ , for policy π_θ :

$$\begin{aligned}\eta_\theta &= \lim_{T \rightarrow \infty} \frac{1}{T} E_\theta \left[\sum_{t=0}^{T-1} Y_{t+1} \mid S_0 = s \right] \\ &= \sum_s d_\theta(s) \sum_a \pi_\theta(a|s) r(s, a)\end{aligned}$$

E_θ denotes expectation under the stationary distribution, d_θ , associated with π_θ .

Background: Differential Value

V_θ is the Differential Value

$$V_\theta(s) = \lim_{T \rightarrow \infty} E_\theta \left[\sum_{t=0}^T \left(Y_{t+1} - \eta_\theta \right) \middle| S_0 = s \right].$$

$V_\theta(s) - V_\theta(s')$ reflects the difference in sum of centered responses accrued when starting in state s as opposed to state s' .

(η_θ is the average reward)

Background: Bellman Equation

Oracle Temporal Difference:

$$\delta_t = Y_{t+1} - \eta_\theta + V_\theta(S_{t+1}) - V_\theta(S_t)$$

Bellman Equation:

$$E_\theta \left[\delta_t \mid S_t \right] = 0$$

$$S_t, A_t, Y_{t+1}, S_{t+1}$$

Background: Bellman Equation

Bellman's equation implies that

$$E \left[\frac{\pi_{\theta}(A_t|S_t)}{\mu(A_t|S_t)} \left(Y_{t+1} - \eta + V(S_{t+1}) - V(S_t) \right) \begin{pmatrix} 1 \\ f(S_t) \end{pmatrix} \right]$$

will be, for all t , for any vector, $f(\cdot)$, of appropriately integrable functions, and appropriate distribution expectation, E , equal to 0 if $\eta = \eta_{\theta}$, $V = V_{\theta}$

Estimating Function

- Construct a nonparametric model for, $V_\theta(s)$, say $f(s)^T v_\theta$, for $f(s)$ a p by 1 vector of basis functions evaluated at s (p is large)

- Solve

$$\mathbb{P}_n \left[\sum_{t=1}^T \frac{\pi_\theta(A_t|S_t)}{\mu(A_t|S_t)} \left(Y_{t+1} - \eta + f(S_{t+1})^T v - f(S_t)^T v \right) \begin{pmatrix} 1 \\ f(S_t) \end{pmatrix} \right]$$

$$=0 \text{ for } \hat{\eta}_\theta, \hat{v}_\theta$$

Overview of Algorithm

- The resulting η and v are functions of θ , denote by $\hat{\eta}_\theta, \hat{v}_\theta$
 - $\hat{\eta}_\theta, \hat{v}_\theta$ are the output of the Critic
- The Actor maximizes $\hat{\eta}_\theta$ over θ to obtain $\hat{\theta}$.
 - this will require repeated calls to the Critic
 - $\hat{\theta}$ is the output of the Actor

Actor

- The objective function for the actor is given by

$$\hat{\eta}_\theta = \mathbb{P}_n \left[\sum_{t=1}^T \frac{\pi_\theta(A_t|S_t)}{\mu(A_t|S_t)} \left(Y_{t+1} + f(S_{t+1})^T \hat{v}_\theta - f(S_t)^T \hat{v}_\theta \right) \right]$$

- We want to construct a policy, π_θ that is bounded away from 0, 1.

Binary action: $\pi_\theta(a|s) = \frac{e^{\theta^T g(s)a}}{1 + e^{\theta^T g(s)}}$

Actor

Chance constraint on θ :

$$T^{-1} \sum_{t=1}^T P^* [p_0 \leq \pi_{\theta}(a|S_t) \leq 1 - p_0] \geq 1 - \alpha$$

for all actions, a and for P^* , a reference distribution.

- This constraint is nonconvex; we relax via Markov inequality.

CRITIC

Write the estimating function as,

$$\mathbb{P}_n \left[\sum_{t=1}^T \frac{\pi_{\theta}(A_t|S_t)}{\mu(A_t|S_t)} \left(Y_{t+1} - \eta + f(S_{t+1})^T v - f(S_t)^T v \right) \begin{pmatrix} 1 \\ f(S_t) \end{pmatrix} \right]$$
$$= \hat{A}_{\theta} \begin{pmatrix} \eta \\ v \end{pmatrix} - \hat{b}_{\theta}$$

To accommodate a large feature vector, the critic minimizes

$$\left\| \hat{A}_{\theta} \begin{pmatrix} \eta \\ v \end{pmatrix} - \hat{b}_{\theta} \right\|^2 + \lambda_c \|v\|^2$$

to obtain $\hat{\eta}_{\theta}$, \hat{v}_{θ}

ACTOR

- The actor obtains $\hat{\theta}$ by maximizing

$$\hat{\eta}_{\theta} = \mathbb{P}_n \left[\sum_{t=1}^T \frac{\pi_{\theta}(A_t|S_t)}{\mu(A_t|S_t)} \left(Y_{t+1} + f(S_{t+1})^T \hat{v}_{\theta} - f(S_t)^T \hat{v}_{\theta} \right) \right]$$

subject to the constraint,

$$\theta^T \Sigma_g \theta \leq \alpha \left(\log((1 - p_0)/p_0) \right)^2$$

$$\Sigma_g = T^{-1} \sum_{t=1}^T E^* \left[g(S_t) g(S_t)^T \right]$$

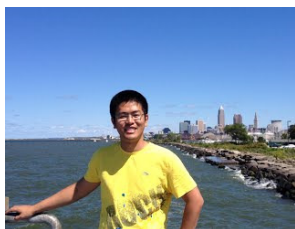
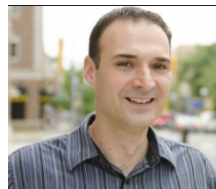
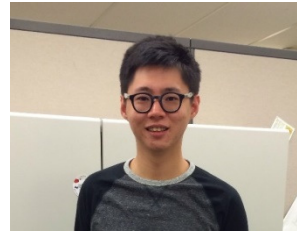
Constructing Policies from Training Data

- We propose an off-line, off-policy actor critic algorithm for learning a treatment policy from a training set.
 - This treatment policy will be a warm-start policy for an online learning algorithm
- Any method should provide confidence intervals/permit scientists to test hypotheses.
- Computational problems.....

Challenges

- How to accommodate/utilize the vast amount of missing data, some of which will be informative.
 - This must be done both for the batch, off-line setting and for online learning.
- How to reduce the amount of self-report data (there are statistical approaches to do this)
- Development of multiple risk predictors both in batch and online setting (including risk for disengagement)
- Measuring burden without causing burden.

Collaborators



Actor

- This chance constraint can be further relaxed to a convex constraint on space of θ by noting

$$1 - T^{-1} \sum_{t=1}^T P^* [p_0 \leq \pi_{\theta}(a|S_t) \leq 1 - p_0] \leq \frac{\theta^T T^{-1} \sum_{t=1}^T E^* [g(S_t)g(S_t)^T] \theta}{(\log((1 - p_0)/p_0))^2}$$

- Our constraint:

$$\alpha \geq \frac{\theta^T T^{-1} \sum_{t=1}^T E^* [g(S_t)g(S_t)^T] \theta}{(\log((1 - p_0)/p_0))^2}$$

Implementation

To approximate the differential value, $V_\theta(s)$, $s=(s_1, \dots, s_{p_1})$, we use features that are all singletons and pairwise products of piecewise linear splines in the set: $\{(s_j - c_{j,k})_+, (c_{j,k} - s_j)_+\} j=1, \dots, p_1, k=1, \dots, 10$.

Thus the dimension of the feature vector, $f(s)$, is $\approx 600p_1^2$

Implementation

The class for π_θ consists of

$$\pi_\theta(a|s) = \frac{e^{(\theta_0 + \theta_1 g_1 + \dots + \theta_q g_q)a}}{1 + e^{\theta_0 + \theta_1 g_1 + \dots + \theta_q g_q}}$$

g_j are features; q is small— in our examples $q=3$

The constraint ($p_0 = \alpha = .05$)

$$\theta^T \Sigma_g \theta \leq .43$$

$$\Sigma_g = T^{-1} \sum_{t=1}^T \mathbb{P}_n [g(S_t)g(S_t)^T]$$