

# A Constrained Viterbi Relaxation for Bidirectional Word Alignment

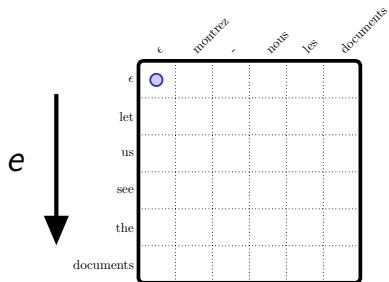
Yin-Wen Chang, Alexander Rush,  
John DeNero and Michael Collins  
ACL 2014

June 25, 2014

# HMM Word Alignment Model

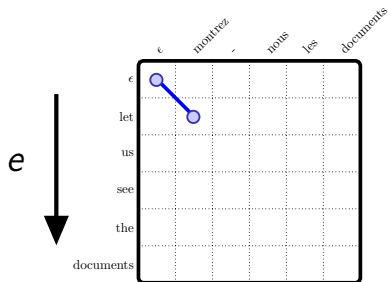
**f:** montrez - nous les documents  
**j:** 1 2 3 4 5

**i:** 1 2 3 4 5  
**e:** let us see the documents



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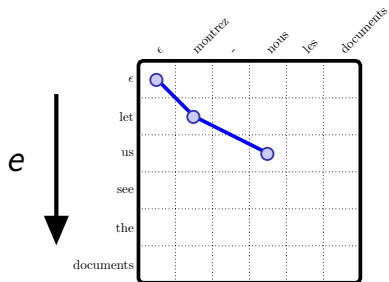
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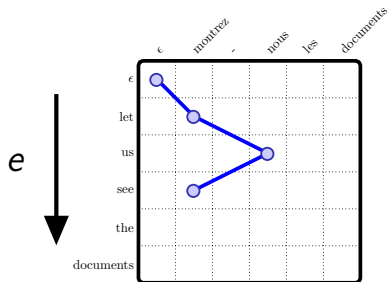
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Blue arrows indicate alignments: from **j:** 1 to **i:** 1, and from **j:** 3 to **i:** 2.



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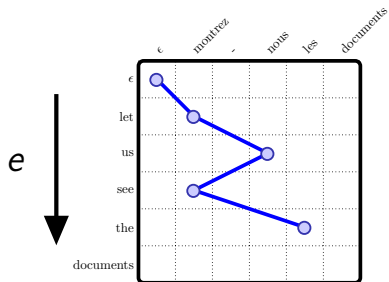
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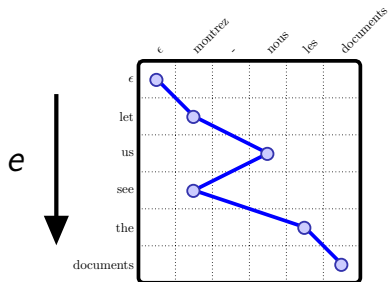
Blue arrows indicate alignments: f1 to i1, f2 to i2, f3 to i3, f4 to i4, and f5 to i5.



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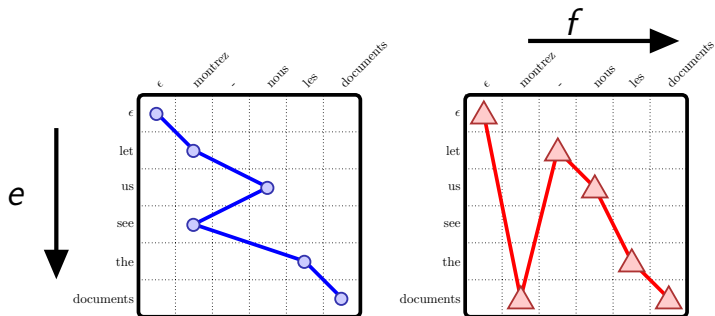
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Blue arrows indicate alignments: f1 to i1, f2 to i2, f3 to i3, f4 to i4, f5 to i5. Additionally, blue arrows show cross-alignments: j1 to i2, j2 to i3, j3 to i4.



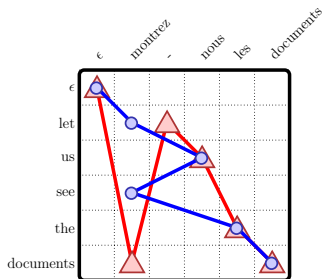
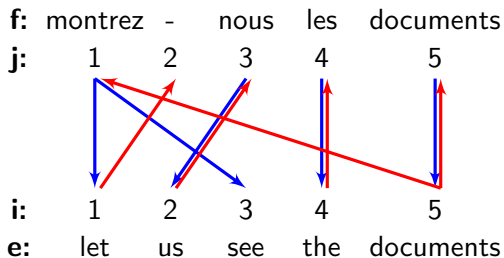
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# HMM Word Alignment Model



## This Work: Bidirectional Alignment

- ▶ Most bidirectional formulations are NP-hard to solve.
- ▶ Previous attempt used dual decomposition and achieved 6% exact solutions (DeNero and Macherey, 2011).
- ▶ **Goal:** increase the number of exact solutions

# Contributions

- ▶ A new relaxation for decoding the bidirectional model, solvable with a variant of Viterbi algorithm.
- ▶ Lagrangian relaxation to enforce the relaxed constraints.
- ▶ General techniques for adding constraints and applying pruning.

# Outline

## Bidirectional Alignment

HMM Word Alignment

Lagrangian Relaxation

## Tightening

Adding Constraints

Pruning

## Results

# Word Alignment: $f \rightarrow e$

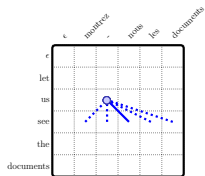
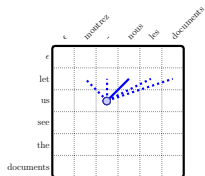
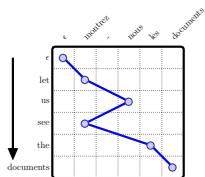
$$f(x; \theta) = \sum_{i,j,j'} \theta(j', i, j) x(j', i, j)$$

- ▶ boundary:  $x(0, 0) = 1$
- ▶ backward consistency:

$$x(i, j) = \sum_{j'=0}^J x(j', i, j)$$

- ▶ forward consistency:

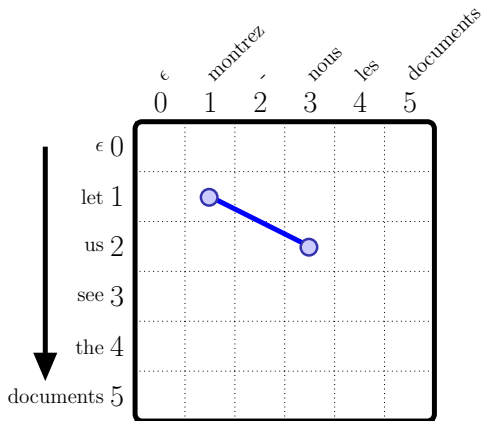
$$x(i, j) = \sum_{j'=0}^J x(j, i+1, j')$$



## Word Alignment Example: $f \rightarrow e$

$$x(1, 2, 3) = 1$$

$$\theta(1, 2, 3) = \log(P(\text{us}|\text{nous})) + \log(P(3|1))$$



# Word Alignment: $e \rightarrow f$

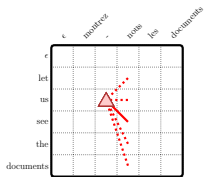
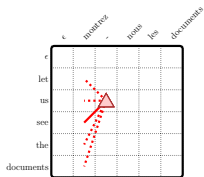
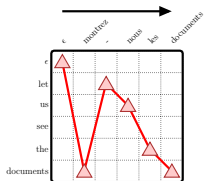
$$g(y; \omega) = \sum_{j, i, i'} \omega(i', i, j) y(i', i, j)$$

- ▶ boundary:  $y(0, 0) = 1$
- ▶ backward consistency:

$$y(i, j) = \sum_{i'=0}^i y(i', i, j)$$

- ▶ forward consistency:

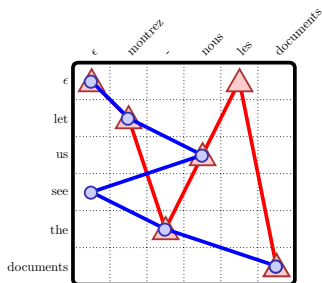
$$y(i, j) = \sum_{i'=0}^i y(i, i', j+1)$$



# Bidirectional Alignment with Full Agreement

**Goal:**

$$x^*, y^* = \arg \max_{x,y} f(x) + g(y) \text{ s.t.}$$
$$x(i,j) = y(i,j) \quad \forall i,j \neq 0$$





# Outline

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Lagrangian Relaxation

## Tightening

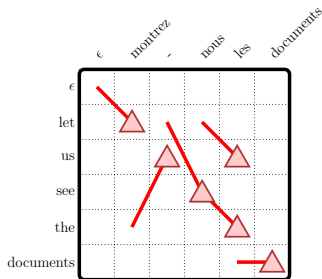
Adding Constraints

Pruning

## Results

# The Relaxed Problem

- ▶  $\mathcal{Y}$ : set of the  $\mathbf{e} \rightarrow \mathbf{f}$  alignment
- ▶  $\mathcal{Y}'$ : set of the  $\mathbf{e} \rightarrow \mathbf{f}$  alignment without the forward constraints
- ▶  $\mathcal{Y} \subset \mathcal{Y}'$



# Lagrangian Relaxation

**Goal:**

$$\begin{aligned}x^*, y^* = & \arg \max_{x \in \mathcal{X}, y \in \mathcal{Y}} f(x) + g(y) \text{ s.t.} \\ & x(i, j) = y(i, j) \quad \forall i, j \neq 0\end{aligned}$$

**Lagrangian dual:**

$$L(\lambda) = \arg \max_{\substack{x \in \mathcal{X}, y \in \mathcal{Y}' \\ x(i, j) = y(i, j)}} f(x) + g'(y; \omega, \lambda)$$

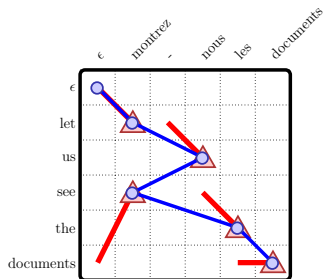
where

$$g'(y; \omega, \lambda) = g(y; \omega, \lambda) - \sum_{i, j} \underbrace{\lambda(i, j)}_{\text{Lagrange multipliers}} \underbrace{\left( y(i, j) - \sum_{i'} y(i, i', j + 1) \right)}_{\text{forward constraints for } y}$$

# Viterbi-style Algorithm for computing $L(\lambda)$

$$\begin{aligned} & \max_{\substack{x \in \mathcal{X}, y \in \mathcal{Y}', \\ x(i,j)=y(i,j)}}} f(x) + g'(y; \omega, \lambda) \\ &= \max_{\substack{x \in \mathcal{X}, y \in \mathcal{Y}', \\ x(i,j)=y(i,j)}}} f(x) + \sum_{i,j} y(i,j) \max_{i'} \omega'(i', i, j) \end{aligned}$$

where  $\omega'(i', i, j) = \omega(i', i, j) - \lambda(i, j) + \lambda(i', j - 1)$



- ▶ Compute the score for each  $y(i, j)$
- ▶ Standard Viterbi update for computing  $x(i, j)$ , adding in the score of  $y(i, j)$

# The Lagrangian Relaxation Algorithm

- ▶ Lagrangian dual is the **upper bound**:

$$L(\lambda) \geq f(x^*) + g(y^*)$$

- ▶ Find tightest upper bound:

$$\min_{\lambda} L(\lambda)$$

- ▶ Minimize by **subgradient**:

1. Set  $(x, y)$  to the arg max of  $L(\lambda)$ .

If  $(x, y)$  satisfies the forward constraint, return  $(x, y)$

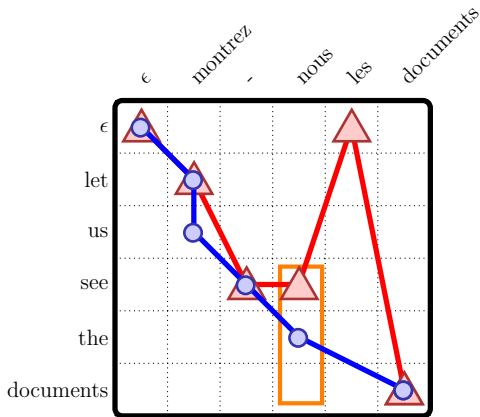
2. Else, update  $\lambda(i, j)$  for all  $i, j$ ,

$$\lambda(i, j) \leftarrow \lambda(i, j) - \eta_t (y(i, j) - \sum_{i'=0}^I y(i, i', j + 1))$$

- ▶ **Certificate of optimality** upon convergence

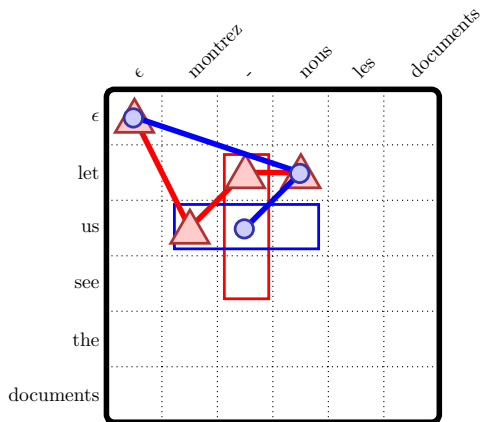
## Extension: Adjacent Agreement

- ▶ A model that allows adjacent matches
- ▶  $x(4, 3) = 1$  because  $y(3, 3) = 1$



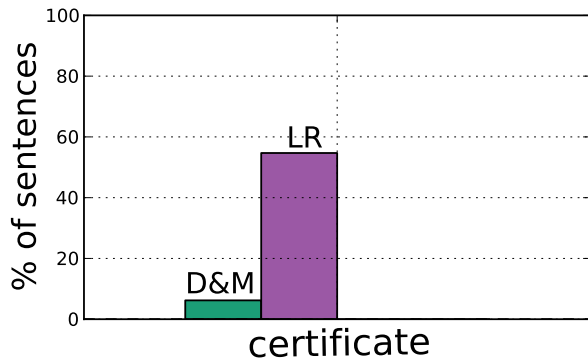
## Extension: Adjacent Agreement

- ▶ A modified Viterbi algorithm with the same complexity



## Preview Results: Lagrangian Relaxation

- ▶ Lagrangian relaxation only guarantee to solve the linear programming relaxation
- ▶ 54.7 % exact solutions





# Outline

## Bidirectional Alignment

HMM Word Alignment

Lagrangian Relaxation

## Tightening

Adding Constraints

Pruning

## Results

## Strategy: Adding Constraints

**Upper bound:**

$$L(\lambda) \geq f(x^*) + g(y^*)$$

**Current gap:**

$$L(\lambda) - (f(x^*) + g(y^*))$$

**Tightening:**

finding a different dual with better gap

$$\text{Find } L'(\lambda) \leq L(\lambda)$$



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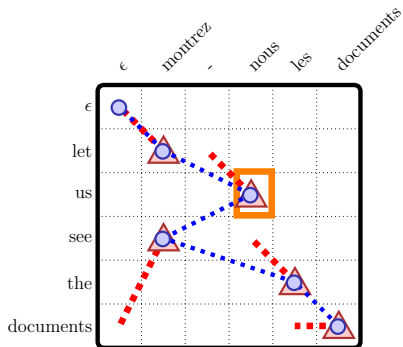
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## Results

# Relaxed Max-marginal

- ▶ Improve efficiency while keeping optimality guarantee
- ▶  $M$ : Relaxed max-marginal values
  - The highest dual value of all alignments using the link  $x(i, j)$
- ▶ Example:  $M(2, 3; \lambda)$



# Exact Coarse-to-Fine Pruning

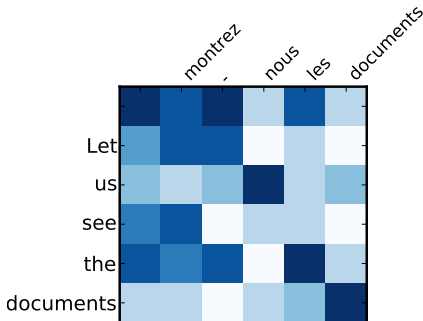
- ▶ We can safely remove an alignment link  $x(i,j)$  if

$$M(i,j; \lambda) < lb$$

- ▶ **Lower bound:**

$$f(x) + g(y) \leq f(x^*) + g(y^*)$$

for some  $x, y$  that is valid



# Exact Coarse-to-Fine Pruning

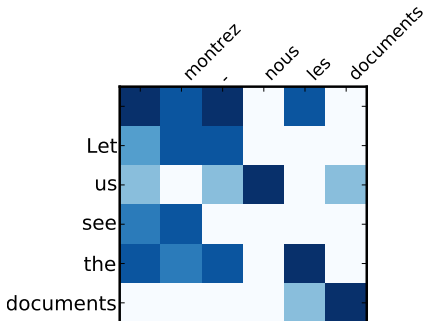
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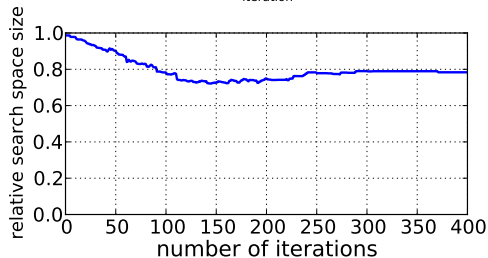
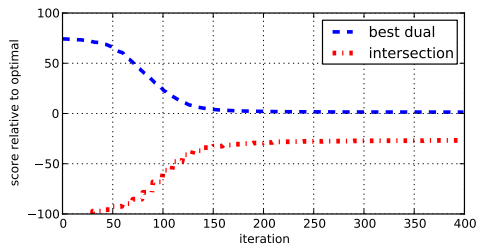
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# Preview Results: Pruning

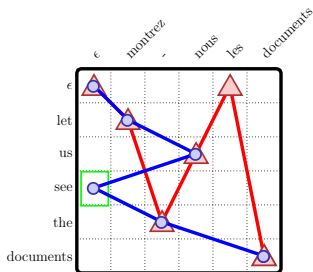




# Finding Lower Bounds

A greedy heuristic algorithm:

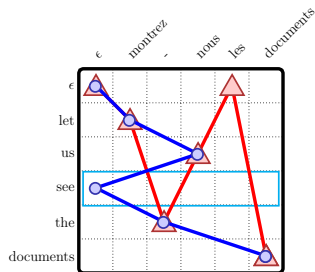
- ▶ Repeat until
  - ▶ there exists no null-aligned word, or
  - ▶ there is no score increase.



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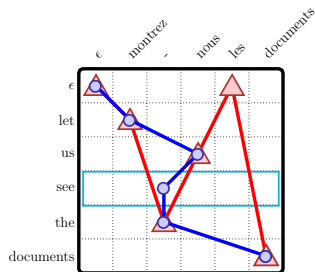
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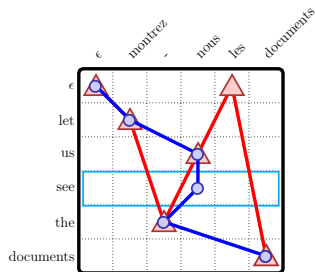
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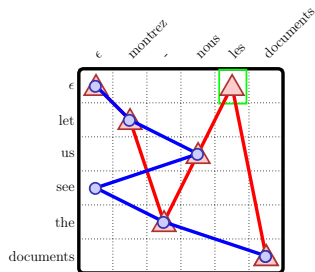
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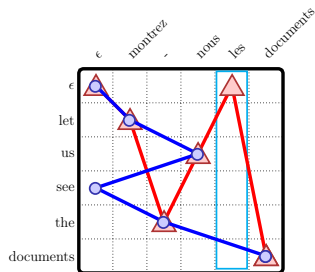
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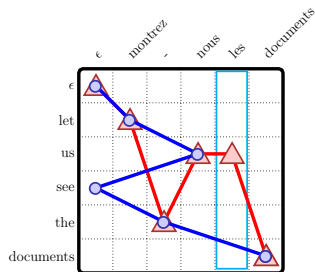
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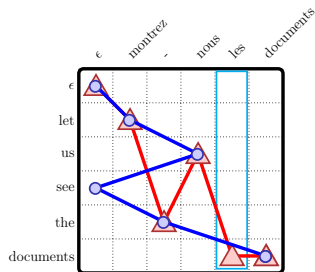
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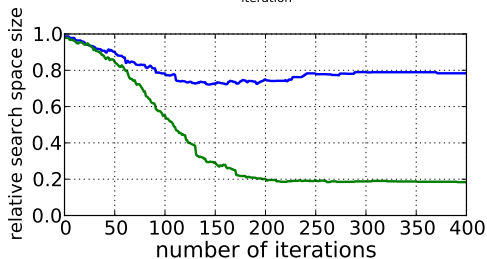
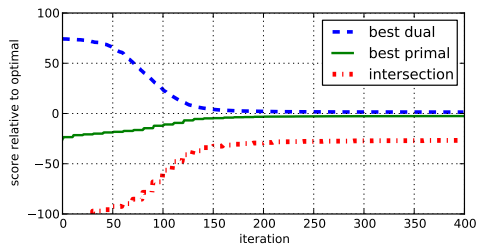
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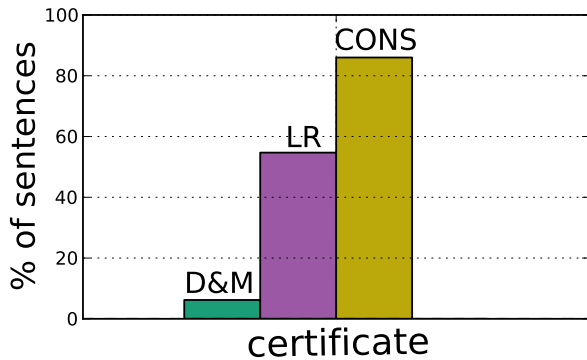
# Results: Coarse-to-Fine Pruning with Good Lower Bound



# Experiments

- ▶ Trained on 6.2 million words of Chinese-English FBIS data
- ▶ Evaluated on 150 sentence pairs of NIST 2002 data
- ▶ Identical to DeNero and Macherey (2011)

## Results: with Adding Constraints and Pruning

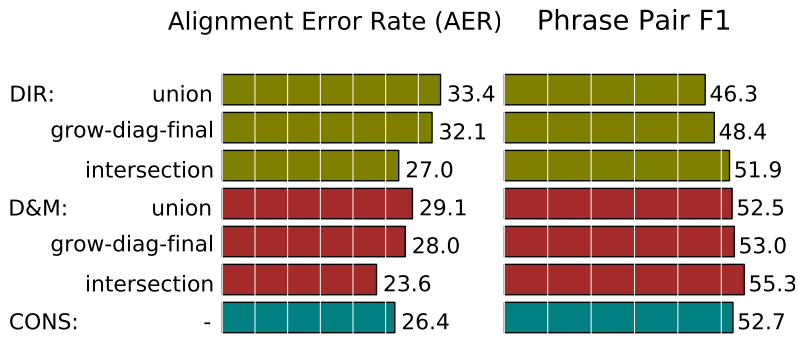


## Results: Speed and Optimal Solutions

	time	certificate (%)
ILP	924.24	100.0
LR	6.33	54.7
CONS	21.08	86.0
D&M	-	6.2

- ▶ ILP: Integer linear programming
- ▶ LR: Our Lagrangian relaxation algorithm
- ▶ CONS: LR with adding constraints
- ▶ D&M: Dual decomposition algorithm by DeNero and Macherey (2011)

## Results: Accuracy



- ▶ DIR: directional alignments
- ▶ When the algorithm does not converge:
  - ▶ D&M uses combination procedures
  - ▶ CONS uses the highest scoring feasible solution

## Conclusion

- ▶ A Lagrangian relaxation algorithm for bidirectional alignment
- ▶ Adding constraints incrementally
- ▶ Coarse-to-fine pruning
- ▶ Convergence on 86% sentences, compared to 6% reported by DeNero and Macherey (2011)
- ▶ **Future work:** apply these techniques to a more flexible model with a wider range of directional matches

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Thank you!